## CHEM 102 Class 5

## Writing ICE tables

(1) Write an ICE table (but don't solve it) for $1.0 \mathrm{M} \mathrm{SO}_{3}$ reacting with $2.0 \mathrm{M} \mathrm{H}_{2} \mathrm{O}$ according to the equation $\mathrm{SO}_{3}(\mathrm{~g})+\mathrm{H}_{2} \mathrm{O}(\mathrm{g})-\mathrm{H}_{2} \mathrm{SO}_{4}(\mathrm{~g})$

|  | $\mathrm{SO}_{3}(\mathrm{~g})$ | $+\mathrm{H}_{2} \mathrm{O}(\mathrm{g})$ | $-\mathrm{H}_{2} \mathrm{SO}_{4}(\mathrm{~g})$ |
| :--- | :---: | :---: | :---: |
| Initial | 1.0 M | 2.0 M | 0 |
| Change | -x | -x | +x |
| Equilibrium | $1.0-\mathrm{x}$ | $1.0-\mathrm{x}$ | x |

(2) Write an ICE table (but don't solve it) for $0.66 \mathrm{~atm} \mathrm{H}_{2}$ reacting with $1.28 \mathrm{~atm} \mathrm{O}_{2}$ according to the equation $2 \mathrm{H}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g})-2 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$

|  | $2 \mathrm{H}_{2}(\mathrm{~g})$ | $+\mathrm{O}_{2}(\mathrm{~g})$ | $-2 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$ |
| :--- | :---: | :---: | :---: |
| Initial | 0.66 atm | 1.28 atm | 0 |
| Change | -2 x | -x | +2 x |
| Equilibrium | $0.66-2 \mathrm{x}$ | $1.28-\mathrm{x}$ | 2 x |

(3) In a container of 10.0 L volume, I mix $1.0 \mathrm{~mol}_{2}, 1.0 \mathrm{~mol} \mathrm{H}_{2}$ and $0.5 \mathrm{~mol} \mathrm{O}_{2}$. Write an ICE table (but don't solve it) for the equilibrium $\mathrm{N}_{2}(\mathrm{~g})+4 \mathrm{H}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g})-\mathrm{N}_{2} \mathrm{H}_{4}(\mathrm{~g})+$ $2 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$

The initial concentrations of the gases are $\mathrm{N}_{2}=1.0 \mathrm{~mol} / 10.0 \mathrm{~L}=0.1 \mathrm{M}, \mathrm{H}_{2}=1.0 \mathrm{~mol} /$ $10.0 \mathrm{~L}, \mathrm{O}_{2}=0.5 \mathrm{~mol} / 10.0 \mathrm{~L}=0.05 \mathrm{M}$

|  | $\mathrm{N}_{2}(\mathrm{~g})$ | $+4 \mathrm{H}_{2}(\mathrm{~g})$ | $\mathrm{O}_{2}(\mathrm{~g})$ | $-\mathrm{N}_{2} \mathrm{H}_{4}(\mathrm{~g})$ | $+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Initial | 0.1 M | 0.1 M | 0.05 M | 0 | 0 |
| Change | -x | -4 x | -x | +x | +2 x |
| Equilibrium | $0.1-\mathrm{x}$ | $0.1-4 \mathrm{x}$ | $0.05-\mathrm{x}$ | x | 2 x |

## Solving equilibrium problems - finding K

(4) In the reaction $2 \mathrm{NO}_{2}(\mathrm{~g}) \mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g})$ the initial concentration of $\mathrm{N}_{2} \mathrm{O}_{4}$ was 0.100 M and $\mathrm{NO}_{2}$ was 0.000 M . At equilibrium, the concentration of $\mathrm{N}_{2} \mathrm{O}_{4}$ was measured as 0.009 M . Calculate $\mathrm{K}_{\mathrm{c}}$.

First set up an ICE table

|  | $\mathrm{NO}_{2}$ | $\mathrm{~N}_{2} \mathrm{O}_{4}$ |
| :--- | :---: | :---: |
| Initial | 0.000 | 0.100 |
| Change | +2 x | -x |
| Equilibrium | $0.000+2 \mathrm{x}$ | 0.009 |

We can see from the last column that x must be $0.100 \mathrm{M}-0.009 \mathrm{M}=0.091 \mathrm{M}$. We can now calculated the equilibrium value of $\mathrm{NO}_{2}$ as $0.000+(2 \times 0.091)=0.182 \mathrm{M}$. Hence the value for $\mathrm{K}_{\mathrm{c}}$ is

$$
\mathrm{K}_{\mathrm{c}}=\frac{\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]}{\left[\mathrm{NO}_{2}\right]^{2}}=\frac{0.009 \mathrm{M}}{0.182 \mathrm{M}^{2}}=0.27
$$

(5) In the reaction $2 \mathrm{NO}_{2}(\mathrm{~g}){ }_{2} \mathrm{~N}_{2} \mathrm{O}_{4}(\mathrm{~g})$ the initial concentration of $\mathrm{NO}_{2}$ was 0.250 M and $\mathrm{N}_{2} \mathrm{O}_{4}$ was 0.000 M . At equilibrium, the concentration of $\mathrm{N}_{2} \mathrm{O}_{4}$ was measured as 0.0133 M. (a) Calculate the equilibrium concentration of $\mathrm{NO}_{2}$ (b) Calculate $\mathrm{K}_{\mathrm{c}}$.

First set up an ICE table

|  | $\mathrm{NO}_{2}$ | $\mathrm{~N}_{2} \mathrm{O}_{4}$ |
| :--- | :---: | :---: |
| Initial | 0.250 | 0.000 |
| Change | -2 x | +x |
| Equilibrium | $0.250-2 \mathrm{x}$ | 0.0133 |

We can see from the last column that x must be 0.0133 M .
(a) We can now calculate the equilibrium value of $\mathrm{NO}_{2}$ as $0.250-2 \mathrm{x}=0.250-0.0266=$ 0.2234 M
(b) Hence the value for $\mathrm{K}_{\mathrm{c}}$ is

$$
\mathrm{K}_{\mathrm{c}}=\frac{\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]}{\left[\mathrm{NO}_{2}\right]^{2}}=\frac{0.0133 \mathrm{M}}{0.2234 \mathrm{M}^{2}}=0.27
$$

Notice that the initial composition was very different than in (4), that the equilibrium amounts of the gases are different but $\mathrm{K}_{\mathrm{c}}$ is the same! It doesn't matter whether you start with reactants, as in (4), or products, as in (5), the same value of K is reached at equilibrium.
(6) Initially, a mixture of $0.100 \mathrm{M} \mathrm{NO}, 0.050 \mathrm{M} \mathrm{H}_{2}$ and $0.100 \mathrm{M} \mathrm{H}_{2} \mathrm{O}$ was allowed to reach equilibrium. There was no $\mathrm{N}_{2}$ present initially. At equilibrium, the concentration of NO was found to be 0.062 M . Calculate $\mathrm{K}_{\mathrm{c}}$.

$$
2 \mathrm{NO}(\mathrm{~g})+2 \mathrm{H}_{2}(\mathrm{~g}){ }_{-} \mathrm{N}_{2}(\mathrm{~g})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{~g})
$$

|  | NO | $\mathrm{H}_{2}$ | $\mathrm{~N}_{2}$ | $\mathrm{H}_{2} \mathrm{O}$ |
| :--- | :---: | :---: | :---: | :---: |
| Initial | 0.100 M | 0.050 M | 0.000 M | 0.100 M |
| Change | -2 x | -2 x | +x | +2 x |
| Equilibrium | 0.062 M |  |  |  |

Note the change in the NO concentration was $(0.100 \mathrm{M}-0.062 \mathrm{M})=0.038 \mathrm{M}$. This represents a decrease of 2 x so $\mathrm{x}=0.019$. Now we know x , we can complete the ICE table

|  | NO | $\mathrm{H}_{2}$ | $\mathrm{~N}_{2}$ | $\mathrm{H}_{2} \mathrm{O}$ |
| :--- | :---: | :---: | :---: | :---: |
| Initial | 0.100 M | 0.050 M | 0.000 M | 0.100 M |
| Change | -0.038 M | -0.038 M | +0.019 M | +0.038 M |
| Equilibrium | 0.062 M | 0.012 M | 0.019 M | 0.138 M |

Finally, we can calculate $\mathrm{K}_{\mathrm{c}}$

$$
\mathrm{K}_{\mathrm{c}}=\frac{\left[\mathrm{N}_{2}\right] \cdot\left[\mathrm{H}_{2} \mathrm{O}\right]^{2}}{[\mathrm{NO}]^{2} \cdot\left[\mathrm{H}_{2}\right]^{2}}=\frac{[0.019] \cdot[0.138]^{2}}{[0.062]^{2} \cdot[0.012]^{2}}=650
$$

## Solving equilibrium problems - given K

(7) In the following reaction, $\mathrm{K}_{\mathrm{p}}=9.3 \times 10^{-7}$ at room temperature. Calculate the equilibrium concentration of $\mathrm{N}_{2} \mathrm{O}_{4}$ in a flask initially containing only 3.00 atm of $\mathrm{NO}_{2}$

$$
2 \mathrm{NO}_{2}(\mathrm{~g}){ }_{-} \mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g})
$$

|  | $\mathrm{NO}_{2}$ | $\mathrm{~N}_{2} \mathrm{O}_{4}$ |
| :--- | :---: | :---: |


| Initial | 3.00 atm | 0.00 atm |
| :--- | :---: | :---: |
| Change | -2 x | +x |
| Equilibrium | $3.00-2 \mathrm{x}$ | x |

Insert into the expression for $\mathrm{K}_{\mathrm{p}}$

$$
K_{p}=\frac{p\left(\mathrm{~N}_{2} \mathrm{O}_{4}\right)}{\mathrm{p}(\mathrm{NO})^{2}}=\frac{\mathrm{x}}{(3.00-2 \mathrm{x})^{2}}=9.3 \times 10^{-7}
$$

Because $\mathrm{K}_{\mathrm{p}}$ is very small, we expect the concentration of $\mathrm{N}_{2} \mathrm{O}_{4}$ to be very small compared with the concentration of $\mathrm{NO}_{2}$ and we can set $3.00-2 \mathrm{x}=3.00$.

$$
\begin{aligned}
\mathrm{K}_{\mathrm{p}} & =\frac{\mathrm{x}}{(3.00)^{2}}=9.3 \times 10^{-7} \\
\mathrm{x} & =8.4 \times 10^{-6} \mathrm{~atm}
\end{aligned}
$$

Check to see if x is less than $5 \%$ of the initial value, $\left(8.4 \times 10^{-6} \mathrm{~atm} / 3.00 \mathrm{~atm}\right) \times 100=$ $2.8 \times 10^{-4} \%$ - assumption OK

Check the value of $K_{p}=8.4 \times 10^{-9} / 3.00^{2}=9.33 \times 10^{-7}$
(8) Iodine molecules dissociate at high temperature according to the reaction

$$
\mathrm{I}_{2}(\mathrm{~g}) \_2 \mathrm{I}(\mathrm{~g})
$$

If $K_{p}=4.5 \times 10^{-4}$ and the reaction initially starts with only $\mathrm{I}_{2}$ with a pressure of 1.000 atm , what is the pressure of $(\mathrm{a}) \mathrm{I}_{2}(\mathrm{~g})$ and $(\mathrm{b}) \mathrm{I}(\mathrm{g})$ at equilibrium?

|  | $\mathrm{I}_{2}(\mathrm{~g})$ | $\mathrm{I}(\mathrm{g})$ |
| :--- | :---: | :---: |
| Initial | 1.000 | 0.000 |
| Change | -x | +2 x |
| Equilibrium | $1.000-\mathrm{x}$ | 2 x |

Insert into the expression for $\mathrm{K}_{\mathrm{p}}$

$$
\begin{aligned}
\mathrm{K}_{\mathrm{p}} & =\frac{\mathrm{p}(\mathrm{I})^{2}}{\mathrm{p}\left(\mathrm{I}_{2}\right)} \\
4.5 \times 10^{-4} & =\frac{(2 \mathrm{x})^{2}}{1.000-\mathrm{x}} \\
1.00-\mathrm{x} \cdot\left(4.5 \times 10^{-4}\right) & =4 \mathrm{x}^{2} \\
4.5 \times 10^{-4}-4.5 \times 10^{-4} \mathrm{x} & =4 \mathrm{x}^{2} \\
4.5 \times 10^{-4} & =4 \mathrm{x}^{2}+4.5 \times 10^{-4} \mathrm{x} \\
0 & =4 \mathrm{x}^{2}+4.5 \times 10^{-4} \mathrm{x}-4.5 \times 10^{-4}
\end{aligned}
$$

This is a quadratic equation with solutions $x=0.0105$ or -0.0106 . The negative solution must be incorrect) otherwise the equilibrium concentration of $\mathrm{I}(\mathrm{g})$ would be negative).
(a) The pressure of $\mathrm{I}_{2}$ at equilibrium is $1.000 \mathrm{~atm}-0.0105 \mathrm{~atm}=0.989 \mathrm{~atm}$
(b) The pressure of I at equilibrium is $2 \mathrm{x}=0.021 \mathrm{~atm}$
(9) $0.05 \mathrm{~mol} \mathrm{H}_{2}(\mathrm{~g})$ and and $0.05 \mathrm{~mol}_{\mathrm{B}}^{2}(\mathrm{~g})$ are placed together in a 5.0 L flask and heated to 700 K . What is the concentration of each substance in the flask at equilibrium if $\mathrm{K}_{\mathrm{c}}=64$ at 700 K ?

$$
\mathrm{H}_{2}(\mathrm{~g})+\mathrm{Br}_{2}(\mathrm{~g})-2 \mathrm{HBr}(\mathrm{~g})
$$

The initial concentrations are $\left[\mathrm{H}_{2}\right]=\left[\mathrm{Br}_{2}\right]=0.05 \mathrm{~mol} / 5.0 \mathrm{~L}=0.01 \mathrm{M}$ and $[\mathrm{HBr}]=0$.

|  | $\mathrm{H}_{2}(\mathrm{~g})$ | $\operatorname{Br}_{2}(\mathrm{~g})$ | $\operatorname{HBr}(\mathrm{g})$ |
| :--- | :---: | :---: | :---: |
| Initial | 0.01 M | 0.01 M | 0 |
| Change | -x | -x | +2 x |
| Equilibrium | $0.01-\mathrm{x}$ | $0.01-\mathrm{x}$ | 2 x |

Insert into the equilibrium expression, assume that x is small in the denominator and solve

$$
\begin{aligned}
\mathrm{K}_{\mathrm{c}} & =\frac{[\mathrm{HBr}]^{2}}{\left[\mathrm{H}_{2}\right] \cdot\left[\mathrm{Br}_{2}\right]}=\frac{(2 \mathrm{x})^{2}}{(0.01-\mathrm{x}) \cdot(0.01-\mathrm{x})} \approx \frac{4 \mathrm{x}^{2}}{0.01 \cdot 0.01}=64 \\
4 \mathrm{x}^{2} & =64 \cdot 0.0001 \\
& =0.0064 \\
\mathrm{x} & =\sqrt{\frac{0.0064}{4}}=0.04
\end{aligned}
$$

Check that 0.04 is small ( $<5 \%$ ) compared with the initial concentrations: $(0.04 / 0.01) \mathrm{x}$ $100=400 \%$. The " $x$ is small" assumption is clearly false here and we must solve a quadratic equation.

$$
\begin{aligned}
\mathrm{K}_{\mathrm{c}} & =\frac{[\mathrm{HBr}]^{2}}{\left[\mathrm{H}_{2}\right] \cdot\left[\mathrm{Br}_{2}\right]}=\frac{(2 \mathrm{x})^{2}}{(0.01-\mathrm{x}) \cdot(0.01-\mathrm{x})}=\frac{4 \mathrm{x}^{2}}{0.0001-0.02 \mathrm{x}+\mathrm{x}^{2}}=64 \\
4 \mathrm{x}^{2} & =64 \cdot\left(0.0001-0.02 \mathrm{x}+\mathrm{x}^{2}\right) \\
& =0.0064-1.28 \mathrm{x}+64 \mathrm{x}^{2} \\
0 & =60 \mathrm{x}^{2}-1.28 \mathrm{x}+0.0064
\end{aligned}
$$

Using the quadratic equation solving formula produces two solutions for x ( 0.008 and 0.0133 ). Clearly the last one is inappropriate here ( $0.01-\mathrm{x}$ would give a negative concentration) so the answer must be 0.008 M .

Therefore, the concentrations are $\left[\mathrm{H}_{2}\right]=\left[\mathrm{Br}_{2}\right]=0.01 \mathrm{M}-0.008 \mathrm{M}=0.002 \mathrm{M}$ and $[\mathrm{HBr}]$ $=2 \mathrm{x}=0.016 \mathrm{M}$

Check $\mathrm{K}_{\mathrm{c}}=(0.016)^{2} /(0.002 \times 0.002)=64$
(10) A mixture consisting of 3.00 mols $\mathrm{H}_{2} \mathrm{O}_{2}, 2.00$ mols $\mathrm{O}_{2}$ and 5.00 mols of $\mathrm{H}_{2}$ in a 5.00 L container was heated to 900 K and allowed to reach equilibrium. Determine the equilibrium amounts of each substance if $\mathrm{K}_{\mathrm{c}}=0.0076$ at 900 K .

$$
\mathrm{H}_{2} \mathrm{O}_{2}(\mathrm{~g})-\mathrm{O}_{2}(\mathrm{~g})+\mathrm{H}_{2}(\mathrm{~g})
$$

Initial concentrations $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]=3.00 \mathrm{mols} / 5.00 \mathrm{~L}=0.600 \mathrm{M},\left[\mathrm{O}_{2}\right]=2.00 \mathrm{mols} / 5.00 \mathrm{~L}=$ $0.400 \mathrm{M},\left[\mathrm{H}_{2}\right]=5.00 \mathrm{mols} / 5.00 \mathrm{~L}=1.000 \mathrm{M}$

|  | $\mathrm{H}_{2} \mathrm{O}_{2}(\mathrm{~g})$ | $\mathrm{O}_{2}(\mathrm{~g})$ | $\mathrm{H}_{2}(\mathrm{~g})$ |
| :--- | :---: | :---: | :---: |
| Initial | 0.600 M | 0.400 M | 1.000 M |
| Change | $?$ | $?$ | $?$ |
| Equilibrium | $?$ | $?$ | $?$ |

We do not yet know whether we are moving towards equilibrium (in which case $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]$ will decrease) or whether we are past equilibrium (in which case $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]$ will increase.

Calculating Q

$$
\mathrm{Q}_{\mathrm{c}}=\frac{\left[\mathrm{O}_{2}\right] \cdot\left[\mathrm{H}_{2}\right]}{\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]}=\frac{(0.4) \times(1.0)}{0.6}=0.67
$$

Since Q is greater than K we are past equilibrium and as we move towards it we will decrease the product concentrations and increase the reactant

|  | $\mathrm{H}_{2} \mathrm{O}_{2}(\mathrm{~g})$ | $\mathrm{O}_{2}(\mathrm{~g})$ | $\mathrm{H}_{2}(\mathrm{~g})$ |
| :--- | :---: | :---: | :---: |
| Initial | 0.600 M | 0.400 M | 1.000 M |
| Change | +x | -x | -x |
| Equilibrium | $0.600+\mathrm{x}$ | $0.400-\mathrm{x}$ | $1.000-\mathrm{x}$ |

$$
\mathrm{K}_{\mathrm{c}}=\frac{\left[\mathrm{O}_{2}\right] \cdot\left[\mathrm{H}_{2}\right]}{\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]}=\frac{(0.4-\mathrm{x}) \times(1-\mathrm{x})}{(0.6+\mathrm{x})}=0.0076
$$

$$
(0.4-x) \times(1-x)=0.0076 \cdot(0.6+x)
$$

$$
0.4-1.4 x+x^{2}=0.00456+0.0076 x
$$

$$
x^{2}-1.4076 x+0.395=0
$$

Solving this gives $\mathrm{x}=1.02$ or 0.387 . Clearly the first answer is inappropriate $\mathrm{so} \mathrm{x}=$ 0.387. Hence, the concentrations at equilibrium are $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]=0.6+0.39=0.99 \mathrm{M},\left[\mathrm{O}_{2}\right]=$ $0.4-0.39=0.01 \mathrm{M}$ and $\left[\mathrm{H}_{2}\right]=1-0.39=0.61 \mathrm{M}$.

Check $\mathrm{K}_{\mathrm{c}}=0.01 \times 0.61 / 0.99=0.0062$ (close to 0.0076 with rounding errors)

